M1.(a) force between two (point) charges is proportional to product of charges ✓ inversely proportional to square of distance between the charges ✓ Mention of force is essential, otherwise no marks. Condone "proportional to charges". Do not allow "square of radius" when radius is undefined. Award full credit for equation with all terms defined.

2

(b) V is inversely proportional to r [or V ∝ (-)1 / r] ✓
 (V has negative values) because charge is negative
 [or because force is attractive on + charge placed near it
 or because electric potential is + for + charge and - for - charge] ✓
 potential is defined to be zero at infinity ✓

Allow 
$$V \times r = constant$$
 for  $1^{st}$  mark.

max	2
-----	---

(c) (i) 
$$Q(=4\pi\varepsilon_0 rV) = 4\pi\varepsilon_0 \times 0.125 \times 2000$$
  
*OR* gradient = Q /  $4\pi\varepsilon_0$  = 2000 / 8  $\checkmark$ 

(for example, using any pair of values from graph) ✓ = 28 (27.8) (± 1) (nC) ✓ (gives Q = 28 (27.8) ±1 (nC) ✓

1
4
_

(ii) at r = 0.20m V = -1250V and at r = 0.50m V = -500Vso pd  $\Delta V = -500 - (-1250) = 750$  (V)  $\checkmark$ work done  $\Delta W$  (= Q $\Delta V$ ) = 60 × 10<sup>-9</sup> × 750 = 4.5(0) × 10<sup>-5</sup> (J) (45 µJ)  $\checkmark$ 

(final answer could be between 3.9 and  $5.1 \times 10^{-5}$ ) Allow tolerance of ± 50V on graph readings. [Alternative for  $1^{st}$  mark:

$$\Delta V = \frac{27.8 \times 10^{-9}}{4\pi\varepsilon_0} \times \left(\frac{1}{0.2} - \frac{1}{0.5}\right)$$
(or similar substitution using 60 nC

instead of 27.8 nC: use of 60 nC gives  $\Delta V = 1620V$ ) ]

(iii) 
$$E\left(=\frac{Q}{4\pi\varepsilon_{0}r^{2}}\right) = \frac{27.8 \times 10^{-9}}{4\pi\varepsilon_{0} \times 0.40^{2}} \checkmark = 1600 (1560) (V \text{ m}^{-1}) \checkmark$$
  
[or deduce  $E = \frac{V}{r}$  by combining  $E = \frac{Q}{4\pi\varepsilon_{0}r^{2}}$  with  $V = \frac{Q}{4\pi\varepsilon_{0}r} \checkmark$   
from graph  $E = \frac{625 \pm 50}{0.40} = 1600 (1560 \pm 130) (V \text{ m}^{-1}) \checkmark$ ]

Use of Q = 30 nC gives 1690 (V m<sup>-1</sup>). Allow ecf from Q value in (i). If Q = 60 nC is used here, no marks to be awarded.

[10]

[1]

2

**M2.**D

**M3.**A

**M4.**B

**M5.**D

M6.(a) force between two (point) charges is proportional to (product of) charges ✓ and inversely proportional to the square of their distance apart ✓

PhysicsAndMathsTutor.com

[1]

[1]

[1]

(b) (i) lines with arrows radiating outwards from each charge ✓ more lines associated with 6nC charge than with 4nC ✓ lines start radially and become non-radial with correct curvature further away from each charge ✓ correct asymmetric pattern (with neutral pt closer to 4nC charge) ✓

3 max

(ii) force 
$$\left(=\frac{Q_1Q_2}{4\pi\varepsilon_0 r^2}\right) = \frac{4.0 \times 10^{-9} \times 6.0 \times 10^{-9}}{4\pi \times 8.85 \times 10^{-12} \times (68 \times 10^{-3})^2}$$

= 4.6(7) × 10<sup>-₅</sup> (N) ✓ Treat substitution errors such as 10<sup>-₅</sup>(instead of 10<sup>-</sup>) as AE with ECF available.

2

(c) (i) 
$$E_4 = \frac{4.0 \times 10^{-9}}{4\pi\epsilon_0 \times (34 \times 10^{-3})^2} (= 3.11 \times 10^4 \text{ V m}^{-1}) \text{ (to the right)} \checkmark$$

For both of 1<sup>st</sup> two marks to be awarded, substitution for **either** or both of  $E_4$  **or**  $E_6$  (or a substitution in an expression for  $E_6 - E_4$ ) must be shown.

$$E_{\varepsilon} \left( = \frac{6.0 \times 10^{-9}}{4\pi\varepsilon_0 \times (34 \times 10^{-3})^2} \right) = (4.67 \times 10^4 \text{ V m}^{-1}) \text{ (to the left) } \checkmark$$

If no substitution is shown, but evaluation is correct for  $E_4$  and  $E_6$ , award one of 1 <sup>st</sup> two marks.

$$E_{\text{resultant}} = (4.67 - 3.11) \times 10^4 = 1.5(6) \times 10^4 \checkmark$$

Unit: V m<sup>-1</sup> (or N C<sup>-1</sup>)  $\checkmark$ Use of  $r = 68 \times 10^{-3}$  is a physics error with no ECF. Unit mark is independent.

4

1

(ii) *direction:* towards 4 nC charge **or** to the left  $\checkmark$ 

**M11.** C

M7.

M8.

M9.

M10.

D

[1]

[12]

[1]

**M12.** A

(b) (i)  $F\left(=\frac{Q_1Q_2}{4\pi\varepsilon_0 r^2}\right) = \frac{4.0 \times 10^{-9} \times 8.0 \times 10^{-9}}{4\pi \times 8.85 \times 10^{-12} \times (80 \times 10^{-3})^2}$ (1) $=4.5(0) \times 10^{-6} \text{N} \text{ (1)}$ 

(ii) (use of 
$$V = \frac{Q}{4\pi\varepsilon_0 x}$$
 gives)  $0 = \left(\frac{4.0 \times 10^{-9}}{4\pi\varepsilon_0 x}\right) - \left(\frac{8.0 \times 10^{-9}}{4\pi\varepsilon_0 (80 \times 10^{-3} - x)}\right)$   
or  $\frac{4}{x} = \frac{8}{80 - x}$  (1)  
 $x = 26.7$ mm (1)

(c) correct directions for E₄ and E₅ (1)
 E₅ approx twice as long as E₄ (1)
 correct direction of resultant R
 shown (1)

[1]

3

4



[10]

3

[1]

**M15.** D

M14.

D

[1]

**M16.** A

[1]

**M17.** D